

Black Box Software Testing

(Professional Seminar)

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Section:21

Combination Testing

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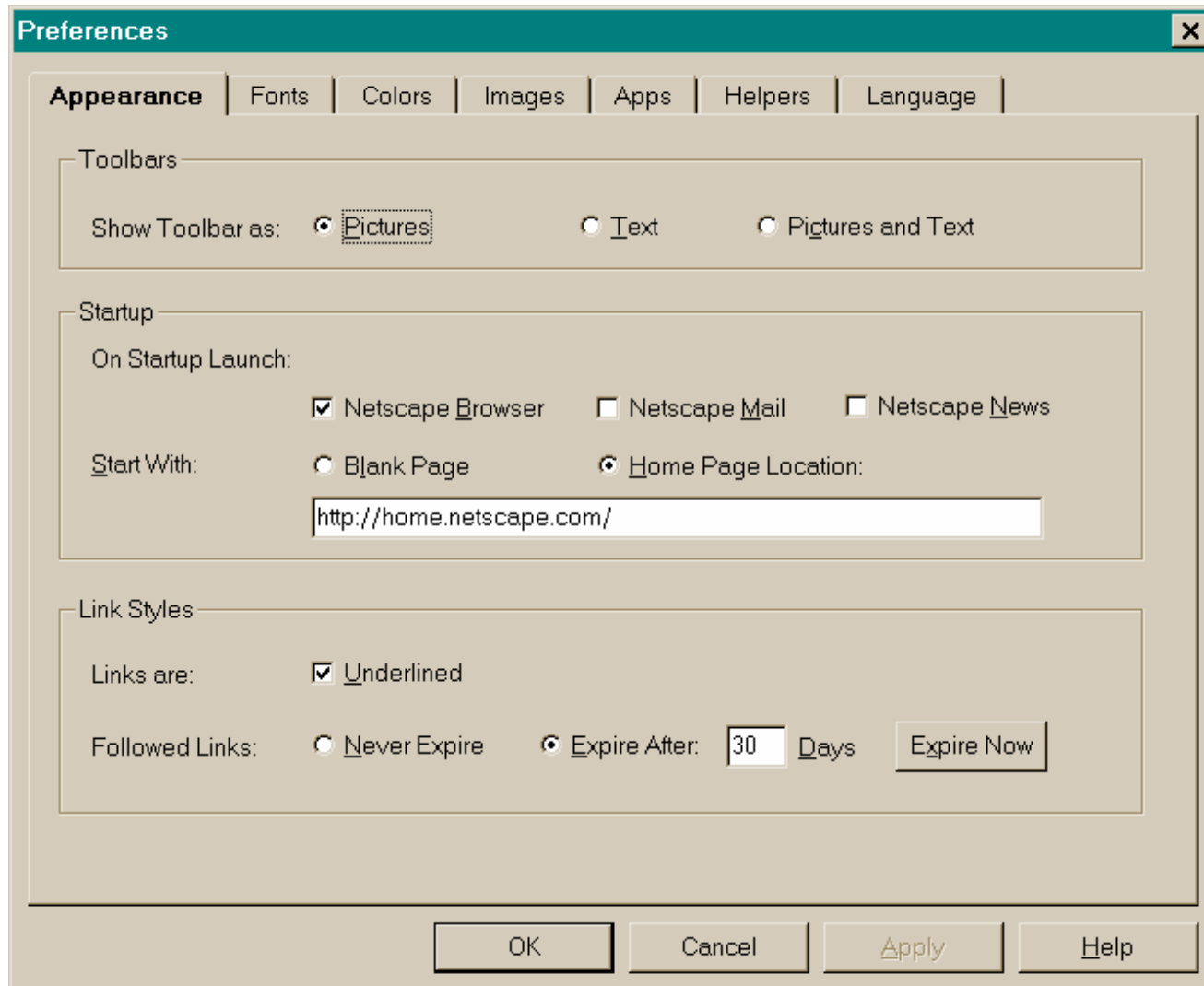
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Combination Chart

	Var 1	Var 2	Var 3	Var 4	Var 5
Test 1	Value 11	Value 12	Value 13	Value 14	Value 15
Test 2	Value 21	Value 22	Value 23	Value 24	Value 25
Test 3	Value 31	Value 32	Value 33	Value 34	Value 35
Test 4	Value 41	Value 42	Value 43	Value 44	Value 45
Test 5	Value 51	Value 52	Value 53	Value 54	Value 55
Test 6	Value 61	Value 62	Value 63	Value 64	Value 65

Testing Variables in Combination



*The
Netscape
Preferences
dialog:*

Testing Variables in Combination

If we just look at the Appearance tab of the Netscape Preferences dialog, we see the following variables:

- Toolbars -- 3 choices (P, T, B)
(*pictures, text* or *both*)
- On Startup Launch -- 3 choices (B, M, N)
(*browser, mail, news*). Each of these is an independent binary choice.
- Start With -- 3 choices (B,V,E)
(*blank* page, home page names a *valid* file, home page name has a *syntax error*)
(Many more cases are possible, but let's keep this simple and ignore that for a few slides)
- Links -- 2 choices (D,U)
(*don't* underline, *underlined*)
- Followed Links -- 2 choices (N,E)
(*never* expire, *expire* after 30 days) (Many more cases are possible)

Testing Variables in Combination

I simplified the combinations by simplifying the choices for two of the fields.

In the Start With field, I used either a valid home page name or a blank name. Some other test cases that could go into this field are:

- file name (name.htm instead of using http:// to define a protocol) on the local drive, the local network drive, or the remote drive
- maximum length file names, maximum length paths
- invalid file names and paths

For combination testing, select a few of these that look like they might interact with other variables. Test the rest independently.

Similarly for the Expire After field. This lets you enter the number of days to store links. If you use more than one value, use boundary cases, not all the numbers in the range.

In multi-variable testing, use partition analysis or other special values instead of testing all values in combination with all other variables' all values.

Testing Variables in Combination

We can create $3 \times 2 \times 2 \times 2 \times 3 \times 2 \times 2 = 288$ different test cases by testing these variables in combination. Here are some examples, from a combination table.

	Toolbars PTB	On Startup, Browser Y/N	On Startup, Mail Y/N	On Startup, News Y/N	Start With BVE	Links DU	Followed NE
Test # 1	P	Y	Y	Y	B	D	N
2	P	Y	Y	N	B	D	E
3	P	Y	N	Y	B	U	N
4	P	Y	N	N	B	U	E
5	P	Y	Y	Y	V	D	N
6	P	Y	Y	N	V	D	E
7	P	N	N	Y	V	U	N
8	P	N	N	N	V	U	E
9	P	N	Y	Y	E	D	N
10	P	N	Y	N	E	D	E
11	P	N	N	Y	E	U	N
12	P	N	N	N	E	U	E

Here are the 288 test cases. Every value of every variable is combined with every combination of the other variables.

1	PYYYBDN	PNYYBDN	TYYYBDN	TNYYBDN	BYYYBDN	BNYYBDN
2	PYYYVDE	PNYYVDE	TYYYVDE	TNYYVDE	BYYYVDE	BNYYVDE
3	PYYEEDN	PNYYEDN	TYYEEDN	TNYYEDN	BYYEEDN	BNYYEDN
4	PYYEBUE	PNYYBUE	TYYEBUE	TNYYBUE	BYYEBUE	BNYYBUE
5	PYYEVUN	PNYYVUN	TYYEVUN	TNYYVUN	BYYEVUN	BNYYVUN
6	PYYEUE	PNYYEUE	TYYEUE	TNYYEUE	BYYEUE	BNYYEUE
7	PYYNBDN	PNYNBDN	TYYNBDN	TNYYNBDN	BYYNBDN	BNYNBDN
8	PYYNVDE	PNYNVDE	TYYNVDE	TNYYNVDE	BYYNVDE	BNYNVDE
9	PYYNEDN	PNYNEDN	TYYNEDN	TNYYNEDN	BYYNEDN	BNYNEDN
10	PYYNBUE	PNYNBUE	TYYNBUE	TNYYNBUE	BYYNBUE	BNYNBUE
11	PYYNVUN	PNYNVUN	TYYNVUN	TNYYNVUN	BYYNVUN	BNYNVUN
12	PYYNEUE	PNYNEUE	TYYNEUE	TNYYNEUE	BYYNEUE	BNYNEUE
13	PYYBDE	PNYYBDE	TYYBDE	TNYYBDE	BYYBDE	BNYYBDE
14	PYYVDN	PNYYVDN	TYYVDN	TNYYVDN	BYYVDN	BNYYVDN
15	PYYEDE	PNYYEDE	TYYEDE	TNYYEDE	BYYEDE	BNYYEDE
16	PYYBUN	PNYYBUN	TYYBUN	TNYYBUN	BYYBUN	BNYYBUN
17	PYYVUE	PNYYVUE	TYYVUE	TNYYVUE	BYYVUE	BNYYVUE
18	PYYEUN	PNYYEUN	TYYEUN	TNYYEUN	BYYEUN	BNYYEUN
19	PYYNBDE	PNYNBDE	TYYNBDE	TNYYNBDE	BYYNBDE	BNYNBDE
20	PYYNVDN	PNYNVDN	TYYNVDN	TNYYNVDN	BYYNVDN	BNYNVDN
21	PYYNEDE	PNYNEDE	TYYNEDE	TNYYNEDE	BYYNEDE	BNYNEDE
22	PYYNBUN	PNYNBUN	TYYNBUN	TNYYNBUN	BYYNBUN	BNYNBUN
23	PYYNVUE	PNYNVUE	TYYNVUE	TNYYNVUE	BYYNVUE	BNYNVUE
24	PYYNEUN	PNYNEUN	TYYNEUN	TNYYNEUN	BYYNEUN	BNYNEUN
25	PYYBDE	PNNYBDE	TYYBDE	TNNYBDE	BYYBDE	BNNYBDE
26	PYYVDN	PNNYVDN	TYYVDN	TNNYVDN	BYYVDN	BNNYVDN
27	PYYEDE	PNNYEDE	TYYEDE	TNNYEDE	BYYEDE	BNNYEDE
28	PYYBUN	PNNYBUN	TYYBUN	TNNYBUN	BYYBUN	BNNYBUN
29	PYYVUE	PNNYVUE	TYYVUE	TNNYVUE	BYYVUE	BNNYVUE
30	PYYEUN	PNNYEUN	TYYEUN	TNNYEUN	BYYEUN	BNNYEUN
31	PYNNBDE	PNNNBDE	TYNNBDE	TNNNBDE	BYNNBDE	BNNNBDE
32	PYNNVDN	PNNNVDN	TYNNVDN	TNNNVDN	BYNNVDN	BNNNVDN
33	PYNNEDE	PNNNEDE	TYNNEDE	TNNNEDE	BYNNEDE	BNNNEDE
34	PYNNBUN	PNNNBUN	TYNNBUN	TNNNBUN	BYNNBUN	BNNNBUN
35	PYNNVUE	PNNNVUE	TYNNVUE	TNNNVUE	BYNNVUE	BNNNVUE
36	PYNNNEUN	PNNNEUN	TYNNNEUN	TNNNEUN	BYNNNEUN	BNNNEUN
37	PYNYBDN	PNNYBDN	TYNYBDN	TNNYBDN	BYNYBDN	BNNYBDN
38	PYNYVDE	PNNYVDE	TYNYVDE	TNNYVDE	BYNYVDE	BNNYVDE
39	PYNYEDN	PNNYEDN	TYNYEDN	TNNYEDN	BYNYEDN	BNNYEDN
40	PYNYBUE	PNNYBUE	TYNYBUE	TNNYBUE	BYNYBUE	BNNYBUE
41	PYNYVUN	PNNYVUN	TYNYVUN	TNNYVUN	BYNYVUN	BNNYVUN
42	PYNYEUE	PNNYEUE	TYNYEUE	TNNYEUE	BYNYEUE	BNNYEUE
43	PYNNBDN	PNNNBDN	TYNNBDN	TNNNBDN	BYNNBDN	BNNNBDN
44	PYNNVDE	PNNNVDE	TYNNVDE	TNNNVDE	BYNNVDE	BNNNVDE
45	PYNNEDN	PNNNEDN	TYNNEDN	TNNNEDN	BYNNEDN	BNNNEDN
46	PYNNBUE	PNNNBUE	TYNNBUE	TNNNBUE	BYNNBUE	BNNNBUE
47	PYNNVUN	PNNNVUN	TYNNVUN	TNNNVUN	BYNNVUN	BNNNVUN
48	PYNNNEUE	PNNNEUE	TYNNNEUE	TNNNEUE	BYNNNEUE	BNNNEUE

Testing Variables in Combination

To simplify this, many testers would test variables in pairs.

That can be useful if you understand specific relationships between the variables, but if you are doing general combination testing, then restricting your attention to pairs is less efficient and less simple than you might expect.

Look at all the pairs you'd have to test, if you tested them all, pair by pair -- 109 of them. This is better than 288, but not much.

Testing Variables in Combination

	Toolbars P/T/B	Browser Y/N	Mail Y/N	News Y/N	Start B/V/E	Links D/U	Followed N/E	TOTAL PAIRS
Toolbars 3 choices	-----	6	6	6	9	6	6	39
Browser 2 choices	-----	-----	4	4	6	4	4	22
Mail 2 choices	-----	-----	-----	4	6	4	4	18
News 2 choices	-----	-----	-----	-----	6	4	4	14
Start 3 choices	-----	-----	-----	-----	-----	6	6	12
Links 2 choices	-----	-----	-----	-----	-----	-----	4	4 -----
Followed 2 choices	-----	-----	-----	-----	-----	-----	-----	<i>109</i>

Testing Variables in Combination

Now consider testing every possible pair, but testing many pairs simultaneously.

We are creating test cases that combine all variables at once, and that assure that every value of every variable is paired with every other value of every other variable.

Each of these test cases covers 21 pairs. In general, each test case that combines N variables includes $N(N-1) / 2$ pairs

	Toolbars PTB	On Startup, Browser Y/N	On Startup, Mail Y/N	On Startup, News Y/N	Start With BVE	Links DU	Followed NE
Test #1	P	Y	Y	Y	B	D	N
2	P	Y	N	N	V	D	E
3	P	N	Y	Y	E	U	E
4	T	Y	N	Y	E	U	N
5	T	N	Y	N	B	D	E
6	T	N	N	Y	V	D	N
7	B	Y	N	N	B	U	E
8	B	N	Y	Y	V	U	E
9	B	N	N	N	E	D	N

Combinations Exercise

Find

Find what: lowercase

Match case

Direction

Up Down

Find Next

Cancel

Here is a simple Find dialog. It takes three inputs:

- Find what: a text string
- Match case: yes or no
- Direction: up or down

Simplify this by considering only three values for the text string, “lowercase” and “Mixed Cases” and “CAPITALS”.

Combinations Exercise

- 1 How many combinations of these three variables are possible?
- 2 List ALL the combinations of these three variables.
- 3 Now create combination tests that cover all possible pairs of values, but don't try to cover all possible triplets. List one such set.
- 4 How many test cases are in this set?

The AETG System: An Approach to Testing Based on Combinatorial Design - Netscape
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Bookmarks Netsite: <https://aetgweb.tipandring.com/papers/AETGieee97.html>

The AETG System: An Approach to Testing Based on Combinatorial Design

Appeared in July 1997 issue of IEEE Transactions On Software Engineering (Vol. 23, No. 7)

By

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Abstract

This paper describes a new approach to testing that uses combinatorial designs to generate tests that cover the pair-wise, triple or n-way combinations of a system's test parameters. These are the parameters that determine the system's test scenarios. Examples are system configuration parameters, user inputs and other external events. We implemented this new method in the AETG

Combinations Exercise

Find has three cases:

L M C (lower, mixed, capitals)

Match has two cases:

Y N (yes, no)

Direction has two cases:

U D (up, down)

1. Total cases is $3 \times 2 \times 2 = 12$

2. Full set has 12 tests

L Y U M Y U C Y U

L Y D M Y D C Y D

L N U M N U C N U

L N D M N D C N D

3. A reduced set is

L Y U

L N D

M Y D

M N U

C Y U

C N D

4. The total is 6

Combination Testing

Imagine a program with 3 variables, V1 has 3 possible values, V2 has 2 possible values and V3 has 2 possible values.

If V1 and V2 and V3 are independent, the number of possible combinations is 12 (3 x 2 x 2)

Building a simple combination table:

- Label the columns with the variable names, listing variables in descending order (of number of possible values)
- Each column (before the last) will have repetition. Suppose that A, B, and C are in column K of N columns. To determine how many times (rows in which) to repeat A before creating a row for B, multiply the number of variable values in columns K+1, K+2, . . . , N.

Combination Testing

Building an all-pairs combination table:

- Label the columns with the variable names, listing variables in descending order (of number of possible values)
- If the variable in column 1 has $V1$ possible values and the variable in column 2 has $V2$ possible values, then there will be at least $V1 \times V2$ rows (draw the table this way but leave a blank row or two between repetition groups in column 1).
- Fill in the table, one column at a time. The first column repeats each of its elements $V2$ times, skips a line, and then starts the repetition of the next element. For example, if variable 1's possible values are A, B, C and $V2$ is 2, then column 1 would contain A, A, blank row, B, B, blank row, C, C, blank row.

Combination Testing

Building an all-pairs combination table:

- In the second column, list all the values of the variable, skip the line, list the values, etc. For example, if variable 2's possible values are X,Y, then the table looks like this so far

A	X
A	Y
B	X
B	Y
C	X
C	Y

Combination Testing

Building an all-pairs combination table:

- Each section of the third column (think of AA as defining a section, BB as defining another, etc.) will have to contain every value of variable 3. Order the values such that the variables also make all pairs with variable 2.
- Suppose variable 2 can be 1,0
- The third section can be filled in either way, and you might highlight it so that you can reverse it later. The decision (say 1,0) is arbitrary.

A	X	1
A	Y	0
B	X	0
B	Y	1
C	X	
C	Y	

Now that we've solved the 3-column exercise, let's try adding more variables. Each of them will have two values.

Combination Testing

The 4th column went in easily (note that we started by making sure we hit all pairs of values of column 4 and column 2, then all pairs of column 4 and column 3.

Watch this first attempt on column 5. We achieve all pairs of GH with columns 1, 2, and 3, but miss it for column 4.

The most recent arbitrary choice was HG in the 2nd section. (Once that was determined, we picked HG for the third in order to pair H with a 1 in the third column.)

So we will erase the last choice and try again:

A	X	1	E	G
A	Y	0	F	H
B	X	0	F	H
B	Y	1	E	G
C	X	1	F	H
C	Y	0	E	G

Combination Testing

We flipped the last arbitrary choice (column 5, section 2, to GH from HG) and erased section 3. We then fill in section 3 by checking for missing pairs. GH, GH gives us two XG, XG pairs, so we flip to HP for the third section and have a column 2 X with a column 5 H and a column 2 Y with a column 5 G as needed to obtain all pairs.

A	X	1	E	G
A	Y	0	F	H
B	X	0	F	G
B	Y	1	E	H
C	X	1	F	H
C	Y	0	E	G

Combination Testing

But when we add the next column, we see that we just can't achieve all pairs with 6 values. The first one works up to column 4 but then fails to get pair EJ or FI. The next fails on GJ, HI

A	X	1	E	G	I
A	Y	0	F	H	J
B	X	0	F	G	J
B	Y	1	E	H	I
C	X	1	F	H	J
C	Y	0	E	G	I

A	X	1	E	G	I
A	Y	0	F	H	J
B	X	0	F	G	I
B	Y	1	E	H	J
C	X	1	F	H	J
C	Y	0	E	G	I

Combination Testing

When all else fails, add rows. We need one for GJ and one for HI, so add two rows. In general, we would need as many rows as the last column has values.

The other values in the two rows are arbitrary, leave them blank and fill them in as needed when you add new columns. At the very end, fill the remaining blank ones with arbitrary values

A	X	1	E	G	I
A	Y	0	F	H	J
				G	J
B	X	0	F	G	I
B	Y	1	E	H	J
				H	I
C	X	1	F	H	J
C	Y	0	E	G	I

Combination Testing

If a variable is continuous but maps to a number line, partition and use boundaries as the distinct values under test. If all variables are continuous, we end up with all pairs of all boundary tests of all variables. We don't achieve all triples, all quadruples, etc.

If some combinations are of independent interest, add them to the list of n-tuples to test.

- With the six columns of the example, we reduced 96 tests to 8. Give a few back (make it 12 or 15 tests) and you still get enormous reduction.
- Examples of “independent interest” are known (from tech support) high risk cases, cases that jointly stress memory, configuration combinations (Var 1 is operating systems, Var 2 is printers, etc.) that are prevalent in the market, etc.

Combination: Interesting Reading

- Cohen, Dalal, Parelius, Patton, “The Combinatorial Design Approach to Automatic Test Generation”, IEEE Software, Sept. 96
<http://www.argreenhouse.com/papers/gcp/AETGissre96.shtml>
- Cohen, Dalal, Fredman, Patton, “The AETG System: An Approach to Testing Based on Combinatorial Design”, IEEE Trans on SW Eng. Vol 23#7, July 97
<http://www.argreenhouse.com/papers/gcp/AETGieee97.shtml>
- **Several other papers on AETG are available at**
<http://aetgweb.argreenhouse.com/papers.html>
- Also interesting: a discussion of orthogonal arrays
<http://www.stsc.hill.af.mil/CrossTalk/1997/oct/planning.html>

Sample Exam Questions

We are going to do some configuration testing on the TI Interactive product. We want to test it on

- Windows 95, 98, and 2000 (the latest service pack level of each)
- Printing to an HP inkjet, a LexMark inkjet, and a Xerox laser printer
- Connected to the web with a dial-up modem (28k), a DSL modem, and a cable modem
- With a 640x480 display and a 1024x768 display
 - » How many combinations are there of these variables?
 - » Explain what an all-pairs combinations table is
 - » Create an all-pairs combinations table
 - » Explain why you think this table is correct.

